

Grade 3

### UNIT 1 | SUB-UNIT 2

# Arrays



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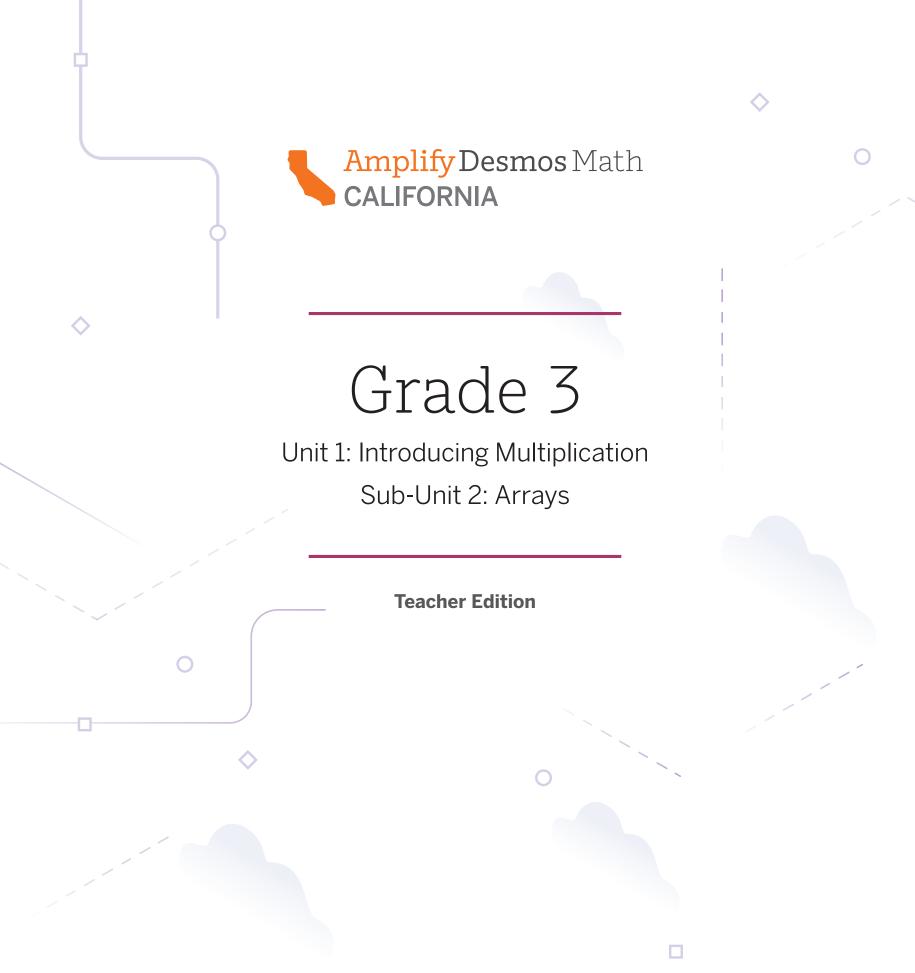
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## **Unit 1** Introducing Multiplication

Students are formally introduce to multiplication and represent and solve problems involving multiplication, including missing factors. Students represent and interpret data using scaled graphs to extend their multiplication work

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### **UNIT 1**

# Introducing Multiplication

#### **Questions for Investigation**

- How does multiplication represent equal groups?
- How do visual models represent multiplication?
- How do different scales affect picture graphs and bar graphs?



#### **Explore:** Finding Equal Groups

Students build curiosity from the beginning of the unit by engaging in a mathematical task that elicits multiple strategies and allows them to apply their own knowledge.



#### Unit Story: My Name Is Harper

In this story, young Harper found her interests and friends at the library. Now she's a grown-up, running that same library.

### Focus on the Big Ideas



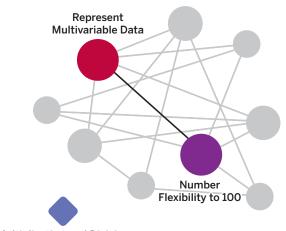
#### CA CCSSM

#### Addressing

3.MD.3, 3.OA.1, 3.OA.3, 3.OA.4, 3.OA.5, 3.OA.7

#### Standards for Mathematical Practice:

SMP.1, SMP.2, SMP.3, SMP.4, SMP.6, SMP.7, SMP.8



**Multiplication and Division** 

Nature Lovers

Every unit has a Unit Story to engage students and help them make connections between math and authentic contexts.



#### **About the Story**

Harper reminisces about her experience as a child, feeling out of place, and then discovering the library for the first time. The library presents itself as a massive, intimidating place with its huge shelves and stacks. But over time, and with the help of her local librarian, Harper becomes more comfortable, even finding friends in other readers she meets there. Now the circle continues as she herself is a librarian, welcoming new readers to her library.



#### Unit Story Read-Aloud

For the Warm-Up of Lesson 1, read aloud the Unit Story. Use the  $\mbox{\bf Presentation Screens}$  for Lesson 1 to display the story images to introduce students to the characters.

#### The Math in the Story

#### Working With Data as an Introduction to Multiplication

As Harper recalls her time in the library, the illustrations provide opportunities for students to see how a group of students with different interests come together as a community and how arrays, as a representation of multiplication, are all around us.

#### Throughout the unit . . .

- Students are introduced to multiplication as an operation to compute equal groups of objects related to the library.
- Students create and look at data representations related to their interests to ask and answer questions.

#### **Math Connections**

Students will connect the math of the unit to the Unit Story in these activities:

- Lesson 1
- · Lesson 11, Activity 1
- Lesson 4, Activities 1 and 2
- Lesson 12, Activity 1
- Lesson 5, Activity 2
- Lesson 14, Activity 1
- Lesson 8, Activity 1

Lesson 9, Activities 1 and 2

· Lesson 16, Activities 1 and 2 Lesson 17. Activities 1 and 2

#### Math Identity and Community

The Unit Story provides an opportunity for students to reflect on their math identity and share their experiences of being a part of a math community. Throughout the unit, you may wish to support students in their mathematical journey by asking them to reflect on the Math Identity and Community questions provided at the start of each lesson.



#### We are a math community.



In the story, Harper realizes it is important to be curious. What are you curious about in math class? (Lesson 5)



Harper feels comfortable being herself at the library. What makes you feel comfortable being yourself in math class? (Lesson 12)

#### **Story Moments**





#### Lesson 1

#### Math Connection

Students take a walk around their school to notice equal groups all around them, just like Harper when she went on a walk to find bugs.





#### **Lesson 4** Activity 2

#### Math Connection

Students write expressions and solve multiplication problems involving book clubs in Harper's class.





#### **Lesson 5** Activity 2

#### Math Connection

Students solve equal-groups problems about the boxes of books the community donated to Harper's classroom.





#### **Lesson 8** Activity 1

#### Math Connection

Students look for arrays in illustrations from the Unit Story and describe how the structure of an array shows equal groups.





#### **Lesson 12** Activity 1

#### Math Connection

Students create a picture graph or a bar graph to represent data Harper collected about her classmates' favorite types of books.





#### **Lesson 17** Activities 1 and 2

#### Math Identity Connection

Students observe data Harper collected to see how many of each type of bug were in her garden and reflect on how they could use a bar graph in everyday life.



### Read-Aloud My Name Is Harper





My name is Harper and for as long as I can remember, I've felt different.

My classmates were always playing the same games, watching the same shows, laughing at the same kind of jokes...

But me? I was happiest by myself.





During recess, I'd stand alone in the yard, watching ants or beetles crawling along the ground.

I loved bugs—things with six eyes, or eight legs, or little wiggly antennas. I loved thinking about their little worlds.

But any time I tried to explain that to my classmates, they'd say my interests were weird.





For a long time, I felt like I was the only person in the whole world that loved these "weird" things. But one day, my mom took me to my local library.

When we walked in, I was amazed.





There were so many books—laid out in piles, stacked in bins, and rolled around in carts. There were dozens of bookcases, going as far as the eye could see. And on each of the bookcases were shelves, each arranged with their own neat rows of books.

I wandered around for so long, I ended up getting lost! I couldn't tell one part of the library from the next. And just when I was about to cry, I looked up. That's when I met Mrs. Park.

Ask: "What do you notice? What do you wonder?"





Mrs. Park was the head librarian. She asked me my name and about the kinds of things I was interested in.

When I told her about the bugs, she didn't laugh. Instead she took me around and showed me how the sections were arranged. Non-fiction. Science. Biology. Insects and Arachnids.

I couldn't believe it! There were shelves upon shelves dedicated to books about different bugs. I had no idea there were so many people interested in the same things I was.





After that, the library became a second home to me.

The more time I spent there, the more I realized there were other people just like me. I don't mean people who love spiders and termites. I mean people who were passionate about what they were interested in. Some of them were even from my class!

Ask: "What do you notice? What do you wonder?"





Like Sam who loved books on dancing.

Or Bethany who loved to read about airplanes. Or Franklin who couldn't get enough stories about mushrooms.

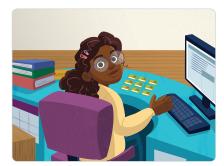
Sometimes, we'd get together and talk about what we were reading.





That's when I began to realize it didn't matter what people thought of the things I cared about. What's important is to always be curious. After all, the world is full of exciting people, places, and things. It would be a shame if we didn't try to explore and understand it.





That was many years ago. These days, I'm the head librarian at my town's library, just like Mrs. Park was.





My favorite part of the job is helping all the different people who come in. I get to hear them talk about their passions and their interests.

If I can, I help them find what they're looking for. It's a powerful thing.

With just the right book, you can change someone's life forever.

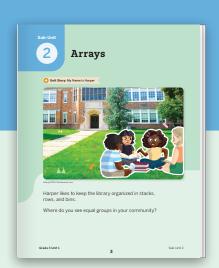
Ask: "What do you notice? What do you wonder?"

### **Sub-Unit 2**

# Arrays

#### **Sub-Unit 2 Goal**

• Represent and solve multiplication problems involving arrays.



### Progression of Big Ideas in Sub-Unit 2

• Lessons 8–11: Students connect Number Flexibility to 100 and Multiplication and Division . They interpret and construct arrays to write multiplication equations and justify their answers.

Sub-Unit 2 Progression	Lesson 8	Lesson 9	Lesson 10	Lesson 11	
Number Flexibility to 100	•	•	•	•	
NS Multiplication and Division	•	•	•	•	

#### **Coming up Next**

• Sub-Unit 3, Lessons 12–18: Represent Multivariate Data Number Flexibility to 100.

## Big Idea Development

GC2 Flexibility to 100 As students progress through Sub-Unit 2, look for these strategies as they develop an understanding of multiplication within 100 by justifying answers using an array.

### Progression of Strategies, Skills, or Language

Progression	For example	
Representing a total number of objects with an array.	Show how this set of dots could be arranged into an array.  2 × 6 2 rows with 6 in each row  The library invites guest readers each month. Their photos are arranged in 3 rows. Each row has 4 photos. How many photos are there?  3 × 4 = ?  There are 12 photos.	
Representing an array with a multiplication expression or equation.		
Determining an unknown total in a multiplication problem involving an array.		
Determining an unknown number of rows or number of objects in each row in a multiplication problem involving an array.	There are 8 rows of crayons in a box. The box has 40 crayons in it. If each row has the same number of crayons, how many crayons are in each row?  8 × ? = 40  There are 5 crayons in each row.	A tray of watercolor paints has 14 colors arranged in an array. Each row has 7 colors. How many rows of colors does the tray have?  ? × 7 = 14  There are 2 rows of colors in the tray.

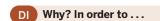
## Searching for Arrays

### Finding, Drawing, and Describing Arrays

Let's identify and describe arrays using what we know about multiplication.

#### Focus on the Big Ideas

- Today's Goal CC2 Number Flexibility to 100 NS Multiplication and Division
  - 1. Language Goal: Describe the relationship between arrays, equal groups, and multiplication. (Speaking and Listening)



multiplication (DI1)

Make sense of and visualize equal groups in relation to



Use precise language when describing arrays (SMP.6)

Using their understanding of factors and products to answer questions. (CC2)

#### **Connections and Coherence**

Students review array structures, identifying them in Unit Story illustrations and describing equal groups. They relate arrays to equal groups, seeing them as rows and columns with equal numbers of objects. Then students create arrays by rearranging dots into 1 or more arrays and describe them using multiplication structures. (SMP.6, SMP.8)

Prior Learning CC4 Squares in an Array

In Grade 2, students learned that a rectangular array contains objects arranged into rows and columns, with the same number of objects in each row and the same number of objects in each column.

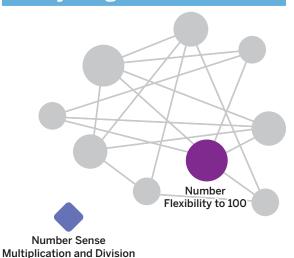
Future Learning CC2 Number Flexibility to 100 NS Multiplication and Division

In Lesson 9, students will represent given multiplication situations with arrays and multiplication expressions.

#### Integrating Rigor in Student Thinking

Students extend their conceptual understanding of multiplication to include arrays, recognizing that arrays show equal groups in rows and columns.

#### Today's Big Ideas



#### Vocabulary

#### **Review Vocabulary**

array

column

row

### **S** CA CCSSM

#### Addressing

#### 3.0A.1

Interpret products of whole numbers, e.g., interpret 5 x 7 as the total number of objects in 5 groups of 7 objects each. For example, describe a context in which a total number of objects can be expressed as  $5 \times 7$ .

Mathematical Practices: SMP.6, SMP.7, SMP.8

**Building On** 

**Building Toward** 

2.0A.4

CA ELD Standards: ELD.PI.3.1, ELD.PI.3.3

### Building Math Identity



How do your classmates support you as a doer of math? How do you support your classmates?

Invite students to reflect on this question as they complete this lesson.

## Lesson at a Glance • 60 min

**S** CA CCSSM: 3.OA.1, SMP.6, SMP.7, SMP.8

#### Warm-Up Fluency

Whole Class | • 10 min

Students use the **How Many Do You See?** routine, in which they develop fluency by describing how they see an arrangement of 12 eggs in a carton. (SMP.7)





#### **Activity 1**

Small Groups | 4 15 min

Students search for and identify arrays in the illustrations from the Unit Story. Then they describe how 1 of the arrays they found shows equal groups. (SMP.6)

**Materials:** Activity 1 PDF, chart paper, markers, Visual Display PDF, *Arrays* 

**Additional Prep** Prepare: *Arrays* chart with markers and chart paper









#### **Activity 2**

1 Independent | 20 min

Students make further connections between equal groups and arrays by rearranging sets of dots to create arrays. They see that a given number of dots can be arranged in more than 1 array and can be represented by more than 1 multiplication expression. (SMP.8)

**Manipulative Kit:** counters (optional), inch tiles (optional)









### **Synthesis**

Whole Class | • 10 min

Students review and reflect on their understanding of arrays and how arrays show equal groups.





#### **Show What You Know**

🔓 Independent | 😃 5 min

Students demonstrate their understanding of arrays by identifying an expression that matches an array.

Materials: Show What You Know PDF







#### **Math Language Development**



Consider using the scaffolds from the *Math Language Development Resources* with Activity 1 to support math language acquisition for your students.



#### Emerging

Students use sentence frames and a word bank to describe arrays with a partner.

Guided questions are provided for you to ask for students to share one-word responses.

#### Expanding =

Students use sentence frames and a word bank to describe arrays with a partner.

Guided questions are provided for you to ask for students to share simple phrases.

#### Bridging |

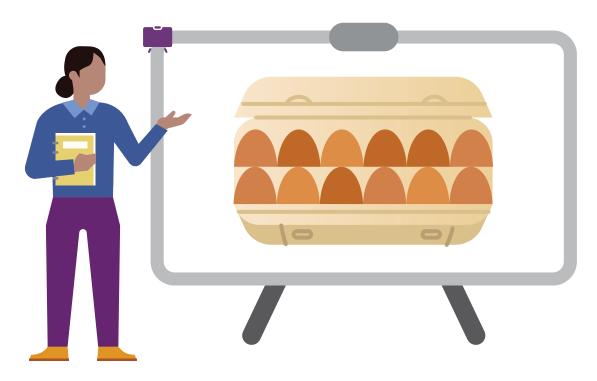
Students use sentence frames and a word bank, if needed, to describe arrays with a partner.

Guided questions are provided for you to ask for students to share responses using longer phrases or complete sentences.

## Lesson 8 Warm-Up

### Warm-Up How Many Do You See?

**Purpose:** Students determine the total number of eggs in a carton to practice decomposing a quantity into equal groups and to review the structure of an array.



**Why this image?** This image is a familiar context and lends itself to connecting equal-groups situations with arrays.

### 1 Launch



**Display** the image and ask, "How many do you see? How do you see them?"

### 2 Connect

**Record** students' responses as they share, honoring all explanations and keeping responses displayed.

Ask, "How does this image relate to what you know about multiplication?"

Say, "The eggs are arranged in an array. You may recall from Grade 2 that an array is an arrangement of objects in rows and columns. Each column has the same number of objects, and each row has the same number of objects. You will continue working with arrays today." Consider using gestures or annotating the image to visually distinguish between horizontal rows and vertical columns.



### Students might say . . . **(**) ELD.PI.3.3.Em, Ex, Br

There are 12 eggs. I know there are 12 eggs in a full carton.

I see 2 rows of eggs, and each row has 6 eggs.  $2 \times 6 = 12$ 

Each egg in the front row has another egg right behind it, so I counted by 2 going across and got 12.

I split the eggs into groups of 4. 4 + 4 + 4 = 12

The eggs are organized in an arroy with

The eggs are organized in an array with 2 rows of 6 eggs. 2 groups of 6 equals 12.





### **Activity 1** Array Hunt

Purpose: Students look for arrays in illustrations from the Unit Story and describe how the structure of an array shows equal groups.

### Launch





Say, "When you have completed Problem 1, choose 1 of the arrays you found and discuss the question in Problem 2 with your small group."

📞 ELD.PI.3.3.Em, Ex, Br

#### Presentation Screens



#### Materials

#### Lesson Resources:

• Distribute the Activity 1 PDF to each group.

#### Classroom materials:

- Refer to the Visual Display PDF, Arrays (sample) (Lesson Resources) and use chart paper and markers to prepare the Arrays chart before the activity.
- **Short on time?** Consider limiting the number of images students analyze for the Array Hunt.
- Multilingual/English Learners Display a list of the words about the context that students might not know, such as illustration and object. Include visuals or translations of each word in languages used by your students. (Reading and Listening) S ELD.PI.3.1 Em, Ex, Br
- **Accessibility:** Visual-spatial processing Guide visualization by having students trace or color-code the rows and columns they see in each array they find.

### 2 Monitor

After students have completed **Problem 2**, refer to the D Differentiation | Teacher Moves table on the following page.

#### If students need help getting started . . .



Ask, "Where do you see an array in this illustration?"

Multilingual/English Learners Emerging, Expanding, and Bridging scaffolds and supports are available in the Math Language Development Resources.



### Connect

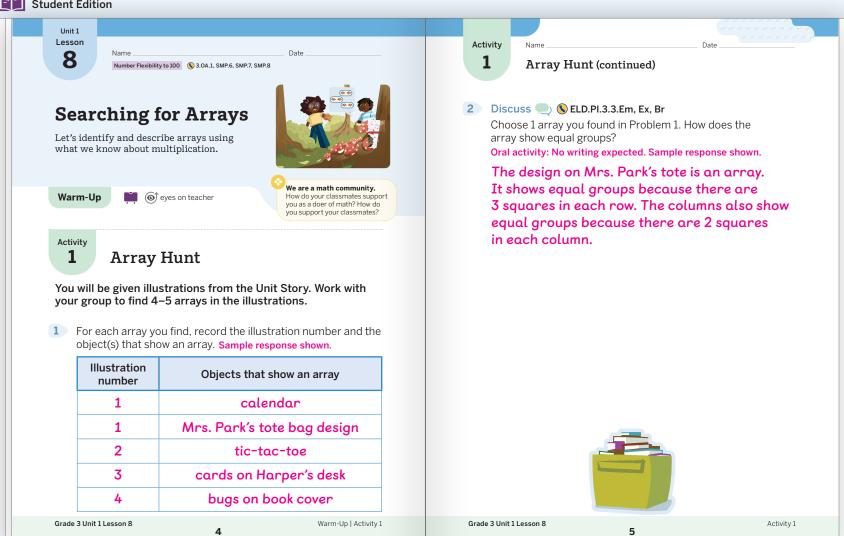


- **Invite 2 or 3 groups of students to share** an array they found. As each group shares, ask:
  - "Where do you see equal groups in this array?"
  - "How does this relate to multiplication?"

Display the Arrays chart. Annotate the array diagrams on the chart to show that columns are vertical and rows are horizontal. Have students describe how the arrays show equal groups in the rows and in the columns by circling the equal groups.



Key Takeaway: Say, "The rows in an array show equal groups because each row has the same number of objects. The columns also show equal groups because each column has the same number of objects."







Look for students who	For example	Provide support	
Almost there Acknowledge that the array has equal groups.	Mrs. Park's tote design has equal groups.	Support Ask, "Where do you see the equal groups in the tote? Draw the tote design in equal groups to make your explanation more precise."	
Show or describe the rows as the equal groups in the array.	The tote design has an equal number of squares going across — 3 on the top and 3 on the bottom.		
Show or describe the columns as the equal groups in the array.		Strengthen Ask, "If you wanted to represent this array with a drawing of equal groups, what would that drawing look like?"	
Show or describe the rows and the columns in the array as having equal groups.	The rows in the tote design show equal groups because there are 3 parts in each row. The columns also show equal groups because there are 2 parts in each column.	Stretch Ask, "What other ways could you arrange the same amount of objects into an array?"	



### **Activity 2** Drawing Arrays

Purpose: Students rearrange groups of dots into arrays and represent them with expressions to connect the representations. They recognize that, sometimes, more than 1 array and expression can represent the same number of objects.

Presentation Screens



#### **Materials**

#### Manipulative Kit:

· Provide students with access to inch tiles and counters. (optional)





**Read aloud** Problems 3 and 4 and answer any clarifying questions.

Say, "You may choose to build arrays with inch tiles or counters if they are helpful. Work on Problems 3 and 4 independently and then discuss Problem 5 with a partner."

**Monitor** 



After students have completed **Problem 4**, refer to the **O** Differentiation | Teacher Moves table on the

#### If students need help getting started . . .

- Ask, "How many equal groups do you see?"
- Ask, "When creating an array, what has to be true?"

**Connect** 



Invite students to share their responses to Problem 4.

**Record** students' arrays and expressions as they share.

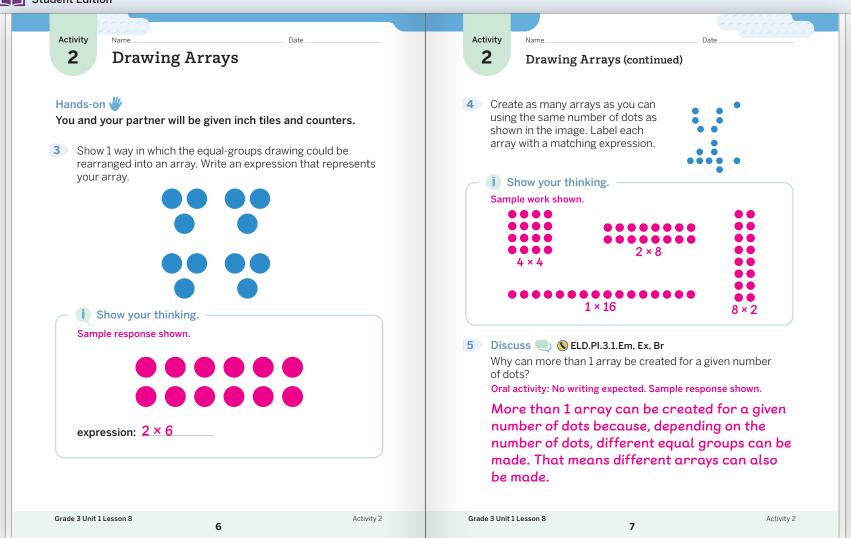




- "What is similar and different about the arrays and expressions that have been shared?"
- "Why can more than 1 array be created for a given number of dots?"
- Multilingual/English Learners Use wait time to allow students to formulate a response. Consider having students rehearse what they will say with a partner before sharing with the group. (S) ELD.PI.3.1 Em, Br, Ex



Key Takeaway: Say, "Numbers can be represented with more than 1 expression and more than 1 array."







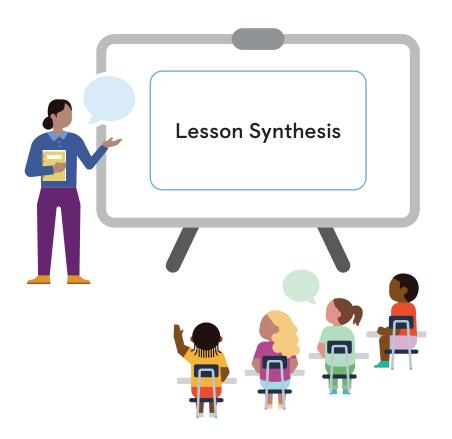
Look for students who	For example	Provide support	
Almost there Use some of the dots or add extra dots to make an array.	or • • • • • • • • • • • • • • • • • • •	Support Ask, "How many dots are in your array? Create an array that has exactly the same number of dots shown in Problem 4."	
Create more than 1 array.	I made an array with 2 rows and 8 columns. Then I started over and made an array with 4 rows and 4 columns.	Strengthen Ask, "How could you know that you created all possible arrays for 16?"	
Recognize that the number of rows and columns in 1 array can be switched to create a different array.	I made an array with 2 rows of 8 dots. I switched the numbers and made another array with 8 rows of 2 dots.	Stretch Ask, "Do you think this could work for any array? Why?"	
Decompose an array into parts and rearrange the parts to form a different array.	I took the 4 columns on the right half of the array and moved them underneath the left 4 columns to make 4 rows of 4 dots.		

#### Presentation Screen



### **Synthesis**

Lesson Takeaway: Arrays can be used to represent multiplication because they show equal groups. There is an equal number of objects in each row, and there is also an equal number of objects in each column.



#### Ask:

- "How are the representations alike? How are they different?"
- "Where do you see equal groups in this array? Describe the array using equal-groups language."
- "What multiplication expression represents these drawings?"

Say, "The rows and columns in this array show equal groups. You can see that there are 4 rows with 5 dots in each row, or there are 5 columns with 4 dots in each column. Because multiplication tells the total number of objects when you have a certain number of equal groups, arrays can be used as another way to represent multiplication."

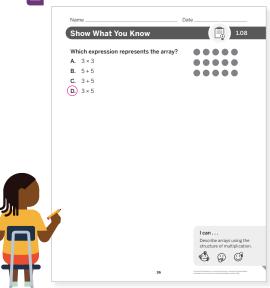
Invite students to refer to the Summary during Practice or anytime during the year.



Students using digital

Lesson 8 Show What You Know





### Today's Goal

- 1. Language Goal: Describe the relationship between arrays, equal groups, and multiplication. (Speaking and Listening)
  - In the Show What You Know, students explain their thinking on how the array shows equal groups.

See the last page of the lesson for differentiation and Math Language Development support.

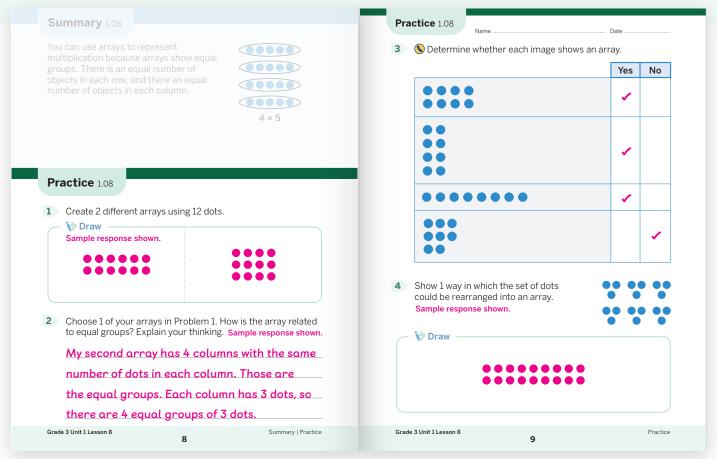
### Practice Independent

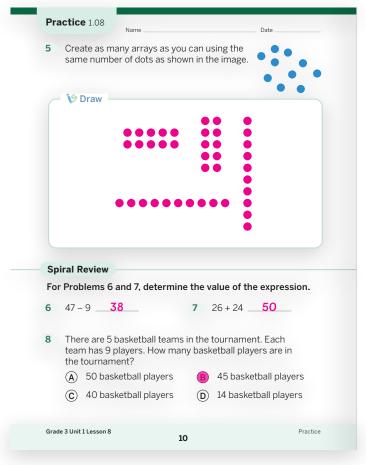
Provide students with sufficient practice to build and reinforce their conceptual understanding, fluency, and application of mathematical topics, assessment practice, and ongoing spiral review.



Students using digital

#### Students using print





Practice Problem Item Analysis			
	Problem(s)	DOK	<b>S</b> CA CCSSM
On-Lesson			
	1, 4	2	3.OA.1, SMP.4
	2, 5	3	3.OA.1, SMP.4, SMP.7
Test Practice	3	2	3.OA.1, SMP.7
Spiral Review			
Fluency	6, 7	1	2.NBT.5, SMP.6
	8	2	3.0A.7, SMP.2



Additional practice can be found in the **Practice Resources**, **Intervention, Extension, and Investigation Resources**, and online resources (item banks, Boost Personalized Learning, and Fluency Practice).

.....

**Lesson Goal:** Describe the relationship between arrays, equal groups, and multiplication.



#### **Support**

Provide targeted intervention for students by using these resources.

**If student work identifies:** an answer other than D

#### Respond:

• Mini-Lesson | • 15 min Writing Expressions for Arrays



Reinforce students' understanding of the concepts assessed by using these resources.

**If student work identifies:** answer D with evidence of describing equal groups

#### Respond:

• Centers | ● 15 min Capture Squares, Stage 5 Cover Up, Stages 10 and 11 Match It, Stage 1



#### **Stretch**

Challenge students and extend their learning with these resources.

**If student work identifies:** answer D with evidence of relating rows and columns to equal group multiplication

#### Respond:

Sub-Unit 2 Extension
 Activities | 4 15 min









Support, Strengthen, and Stretch learning by assigning these digital resources that adjust to each student's current level of skill and understanding.

• Boost Personalized Learning • Fluency Practice • Math Adventures

#### **Math Language Development**

- Use the **Math Language Development Resources** for further language support with all your students, including those building English proficiency.
  - English/Spanish cognates e.g. column/columna
  - English/Spanish Glossary e.g. array/formación
  - Frayer Model templates
  - Math Language Routine display structures
  - Vocabulary routines



#### **Professional Learning**

In previous grades, students saw examples of arrays, such as 10-frames and arrangements of counted objects. How does that previous experience support students' work with equal groups in arrays in this lesson?

## 9

## **Arrays of Flavor**

# **Exploring the Commutative Property of Multiplication**

Let's look for patterns to make conjectures about multiplication.

#### Focus on the Big Ideas

- Today's Goals CC2 Number Flexibility to 100 NS Multiplication and Division
  - 1. Goal: Recognize the Commutative Property of Multiplication.
  - 2. Language Goal: Describe how the order of factors affects the product. (Speaking and Listening)



Recognize that the product of 2 factors is the same, independent of order (DI2)



Look for patterns and structure in arrays (SMP.7)



Identifying equivalent multiplication expressions. (CC2)

#### **Connections and Coherence**

Students explore array structures and learn the **Commutative Property of Multiplication**. They create and compare arrays and expressions with the same total objects. Students notice that rearranging arrays does not change the total. They also analyze expressions with the same product, concluding that the order of factors does not affect the result. (SMP.7, SMP.8)

In Grades 1 and 2, students explored and applied the Commutative Property of Addition. In Lessons 7 and 8, students connected multiplication expressions and equations with equal-groups drawings, arrays, and situations.

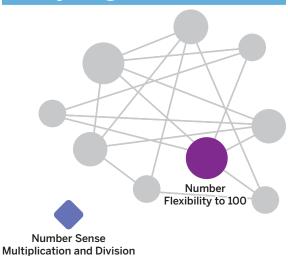
> Future Learning CC2 Number Flexibility to 100

In Lessons 10 and 11, students will apply what they know about multiplication to solve problems with unknown factors and unknown products in different contexts.

### **Integrating Rigor in Student Thinking**

Students build their **conceptual understanding** of the Commutative Property of Multiplication and then **apply** their understanding of multiplication to make generalizations about the commutative structure of multiplication.

### **Today's Big Ideas**



#### Vocabulary

#### **New Vocabulary**

**Commutative Property of Multiplication** 

#### **Review Vocabulary**

factor

product

### CA CCSSM

#### Addressing

#### 3.0A.5

Apply properties of operations as strategies to multiply and divide.

Also Addressing: 3.0A.1

Mathematical Practices: SMP.7, SMP.8

CA ELD Standards: ELD.Pl.3.1. ELD.Pl.3.3

### **Building Math Identity**

O I am a doer of math.

Where do you see arrays in the world around you?

Invite students to reflect on this question as they complete this lesson.

### Lesson at a Glance • 60 min

#### Why digital?

Students test their class conjecture to explore the Commutative Property of Multiplication and receive responsive feedback in real time.

### **S** CA CCSSM: 3.OA.1, 3.OA.5, SMP.7, SMP.8

## Warm-Up Fluency Whole Class | 4 10 min

Students use the **Notice and Wonder** routine to share what they notice and wonder about an array. **(SMP.7)** 

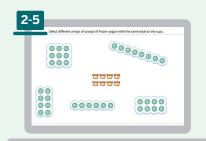


#### **Activity 1**

♣ Pairs | ● 20 min

Students create expressions and arrays that represent the same total amount. They then make observations about the expressions and arrays to support them in forming conjectures. (SMP.7)

Students using print: counters (as needed)



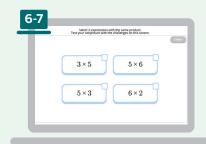
#### **Activity 2**

**♣** Pairs | **●** 15 min

Students test their class conjecture by selecting pairs of expressions that represent the same product. They notice that multiplication is commutative — changing the order of factors results in the same product. During the Connect, students are introduced to the term <a href="Commutative">Commutative</a> <a href="Property of Multiplication">Property of Multiplication</a>. (SMP.8)

Students using print: counters (as needed)

Materials: Arrays chart (from Lesson 8)



### **Synthesis**

Whole Class | **4** 10 min

Students review and reflect on the connections between arrays and the Commutative Property of Multiplication.



#### **Show What You Know**

👗 Independent | 😃 5 min

Students demonstrate their understanding of the Commutative Property of Multiplication by selecting 2 expressions with the same product.

Students using print: Show What You Know PDF



#### **Math Language Development**



Consider using the scaffolds from the *Math Language*Development Resources with Activity 2 to support math language acquisition for your students.



#### Emerging

Students use a graphic organizer, sentence frames, and a word bank to prove the conjecture.

Guided questions are provided for you to ask for students to gesture or share one-word responses.

#### Expanding

Students use a graphic organizer, sentence frames, and a word bank to prove the conjecture.

Guided questions are provided for you to ask for students to share simple phrases.

#### Bridging

Students use a graphic organizer, sentence frames, and a word bank, if needed, to prove the conjecture.

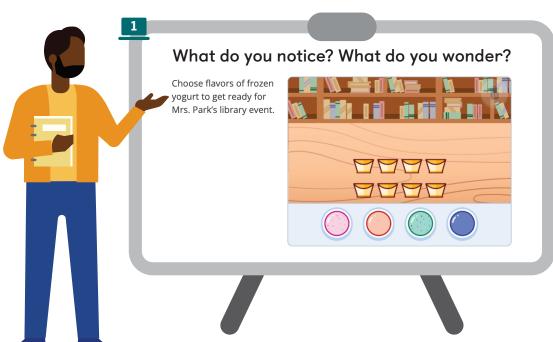
Guided questions are provided for you to ask for students to share responses using longer phrases or complete sentences.

## Warm-Up Notice and Wonder Fluency

**Purpose:** Students examine an array to prepare for exploring the Commutative Property of Multiplication.

Students using print





### 1 Launch

**Display** the empty cups.

**Say**, "Mrs. Park is setting up cups of frozen yogurt for a library event."

**Use the Notice and Wonder routine.** 

**Use the Think-Pair-Share routine.** Ask, "What do you notice? What do you wonder?"

### 2 Connect

Record students' responses. As they share, demonstrate adding frozen yogurt scoops to the cups.

**Ask**, "How could you determine the total number of frozen yogurt scoops that fit in the array of cups?"



### Students might say . . . . . . S ELD.PI.3.1.Em, Ex, Br

I notice that if you add more than 8 scoops of frozen yogurt, the yogurt lands on the table.

I notice that the cups are organized in an array with 2 rows and 4 in each row.

I wonder why more cups aren't added when you add more frozen yogurt scoops.

I wonder what would happen if you organized the cups in a different way.

### **Activity 1** Scoops of Frozen Yogurt

**Purpose:** Students make observations about different arrays with the same total to make a conjecture about how the order of the factors affects the product.

### Students using print

Additional Print Materials

Manipulative Kit:

 Provide each pair with access to counters (as needed).



### 1 Launch



**Display** the arrays.

**Say**, "To set up for the library event, Mrs. Park wants to put 1 scoop of frozen yogurt into each cup. Select different arrays of scoops of frozen yogurt with the same total as the cups."

**Invite pairs to share** their responses and strategies from Screen 2.

Say, "Continue on to Screen 3 to create 2 different arrays of cups that could hold the number of frozen yogurt scoops shown. When you are finished, share your arrays with your partner and discuss what you notice and wonder about the arrays and expressions. Then continue on to Screen 4."



**Accessibility: Visual-spatial processing** Provide access to counters for students to model their arrays.

### 2 Monitor



After students have completed **Screen 3**, refer to the **O Differentiation | Teacher Moves** table on the following page..

- 3-4 If students need help getting started . . .
  - Ask, "How could you use what you did on Screen 2 to help you organize the same number of scoops in a different array?"
  - Ask, "How could you use what you know about rows to create an expression to represent your array?"

### 3 Connect



Display the arrays.

**Use the Notice and Wonder routine** by asking students what they notice and wonder about the arrays and expressions. **SELD.PI.3.1.Em, Ex, Br** 

**Ask**, "What do you notice about the total number of scoops in each array? Where do you see each factor represented in each array?"

### MLR8: Discussion Supports — Make a Conjecture

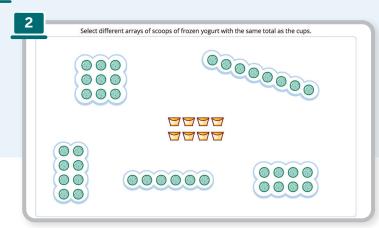
Ask, "Now, you will make a conjecture. A conjecture is a statement you believe is true based on the information you have. What conjectures could you make about multiplication using patterns you notice in these arrays?" **SELD.PI.3.3.Em, Ex, Br** 

Have students share their conjectures to begin creating and recording a class conjecture on the board. Then discuss the following questions:

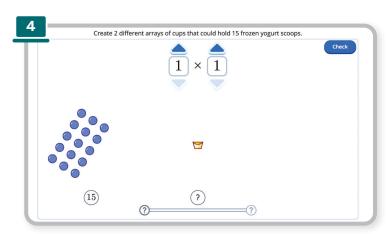
- "How do you know whether our conjecture is always true?"
- "Are there any examples that show this conjecture is false?"



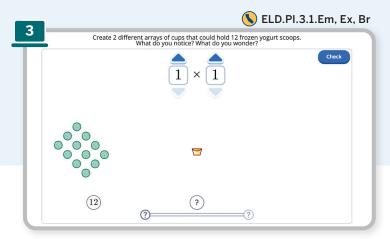
**Key Takeaway:** Say, "You will continue to explore patterns in multiplication in the next activity by testing our class conjecture."



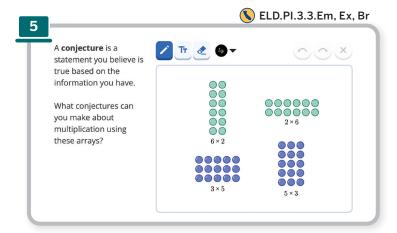
Students select arrays that represent the same total.



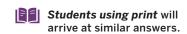
Students create 2 arrays that represent the same total.



Students create 2 arrays that represent the same total and compare their arrays with a partner.



Students make conjectures about the relationship between multiplication and arrays.



### Differentiation | Teacher Moves

Land Const. dealer ha	F
Look for students who	For example

I notice that different arrays

can show a total of 12.

▲ **Support** Ask, "What do you notice is similar about the arrays? What is different?"

Provide support . . .

Notice that some arrays look similar but rotated, with the number of rows and the number of objects in each row switched.

Notice that there are a variety of arrays

that show the same total.

I notice that these arrays look the same, but one is rotated. The left array shows 3 rows of 4, and the right array shows 4 rows of 3.

Notice that some expressions represent the same total number of objects and have the same factors, but the factors are in different orders. I notice that when the same factors are used, they are sometimes in a different order even though the totals are the same.

Strengthen Ask, "What do the factors in the expressions represent in the arrays?"

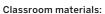
### **Activity 2** Testing Conjectures

Purpose: Students test the class conjecture by selecting expressions that have the same value, recognizing that the factors can be multiplied in any order and the product will be the same.

#### **Additional Print** Materials

#### Manipulative Kit:

 Provide each pair with access to counters (as needed).



· Record on the Arrays chart (from Lesson 8) during the Connect.



### Launch



6 **Display** the expressions.

Say, "As you work on Screen 6, consider our class conjecture. Select 2 expressions with the same product. Complete as many challenges as you have time for. Determine if the class conjecture is always true."

Have students work on Screen 6, and ensure all students complete the first 3 challenges.

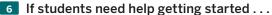


Accessibility: Visual-spatial processing Provide access to counters for students to model the expressions.

### 2 Monitor

While students complete **Screen 6**, refer to the **ODIFFERENTIAL OF SCREEN MOVES** table on the following page.





- · Ask, "What do you notice about the expressions?"
- Ask, "How could you use what you know about arrays to help you select expressions with the same product?"
- Multilingual/English Learners Emerging, Expanding, and Bridging scaffolds and supports are available in the Math Language Development Resources.



### Connect

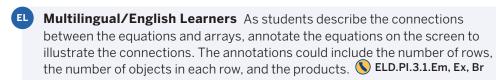


6 Pause: Screen 6.

Use the Think-Pair-Share routine. Ask, "Is the class conjecture always true? How do you know?" ( ELD.PI.3.1.Em, Ex, Br

7-8 **Display** the equations.

- "How do you know that each of these equations is true?"
- "How can arrays help you prove that changing the order of the factors does not change the product?"

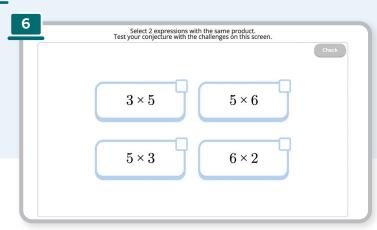


8 Define The Commutative Property of Multiplication. Demonstrate determining the product of  $3 \times 5$  and  $5 \times 3$  using the multiplication table. Demonstrate with additional multiplication expressions as needed.

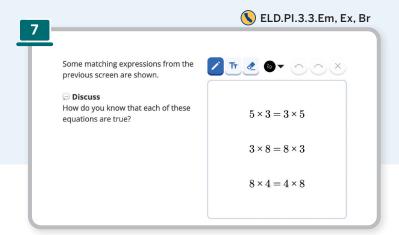
**Record** and annotate the expressions to represent the arrays on the *Arrays* chart.



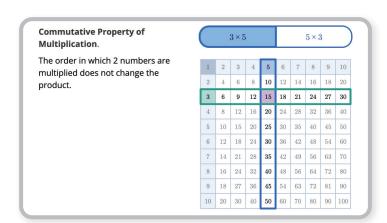
Key Takeaway: Say, "Arrays can help show that factors can be multiplied in any order and the product will be the same. This is called the **Commutative** Property of Multiplication.'



Students test their class conjecture by selecting 2 multiplication expressions that represent the same product.



Students reflect on their class conjecture.



Students using print will arrive at similar answers.

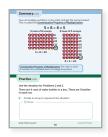
### Differentiation | Teacher Moves

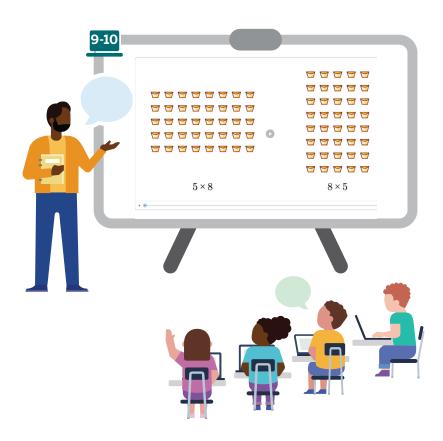
Look for students who	For example	Provide support
Almost there: Select expressions based on 1 factor being the same.	I selected 5 × 3 and 5 × 6 because both expressions have 5 as one of the factors.	<b>Support</b> Ask, "What is the product of each of these expressions?"
Select expressions based on both factors being the same.	I selected 5 × 3 and 3 × 5 because both expressions have a 5 and a 3.	Strengthen Ask, "How do you know the expressions you selected have the same product?"
Select expressions based on the product.	I determined the product of all 4 expressions and selected 3 × 5 and 5 × 3 because they both have a product of 15.	Strengthen Ask, "What do you notice about the factors in the expressions you selected? How does this help you test our conjecture?"
Select expressions based on the Commutative Property of Multiplication.	I selected 3 × 5 and 5 × 3 because I know that it doesn't matter what order the factors are in; when you multiply them, you will get the same product.	Stretch Ask, "Would this also be true for expressions with greater factors, such as 43 × 2 and 2 × 43? How do you know?"

### **Synthesis**

**Lesson Takeaway:** The order in which numbers are multiplied does not change the product. This is called the **Commutative Property of Multiplication**.

#### Students using print





**Display** the array.

**Ask**, "Jada and Diego are determining the product of  $5 \times 8$ . Jada says she can determine the product by counting by 8. Diego says he can determine the product by counting by 5. Who do you agree with and why?"

**Use the Think-Pair-Share routine.** Ask, "How can knowing the Commutative Property of Multiplication be helpful when determining the product of 2 numbers?"

10 Play the animation.

**Say**, "Similar to adding 2 numbers in any order and getting the same sum, you can multiply numbers in any order and get the same product."

Formalize vocabulary: Commutative Property of Multiplication The order in which 2 numbers are multiplied does not change the product.

(optional) **Consider using the Total Physical Response routine** by inviting students to demonstrate the changing of order of factors by crossing and uncrossing their hands. **SELD.PI.3.1 Em, Ex, Br** 

Refer to the *Math Language Development Resources* for more vocabulary support.

**Invite** students to refer to the **Summary** during Practice or anytime during the year.

### **Show What You Know**

Independent | 5 min |
Suggested Pacing: Screens 10-11

Students using print (Show What

You Know PDF)



#### Students using digital



#### **Today's Goals**

- **1. Goal:** Recognize the Commutative Property of Multiplication.
  - In the Show What You Know, students determine which expressions have the same product using the commutative structure of multiplication.
- **2.** Language Goal: Describe how the order of factors affects the product. (Speaking and Listening)
  - In the Show What You Know, students describe how the order of the factors does not affect the product.



See the last page of the lesson for differentiation and Math Language Development support.

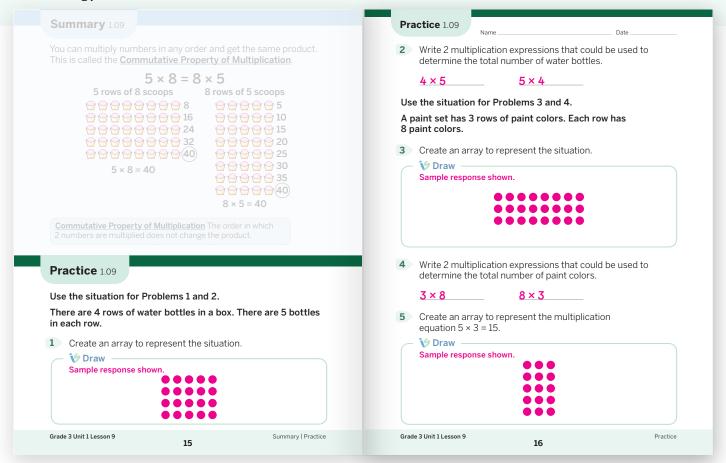
### Practice Independent

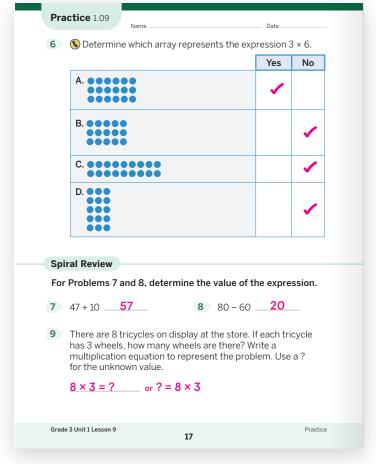
Provide students with sufficient practice to build and reinforce their conceptual understanding, fluency, and application of mathematical topics, assessment practice, and ongoing spiral review.

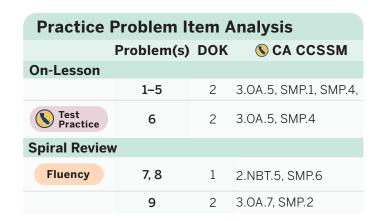


Students using digital

#### Students using print









**Lesson Goal:** Recognize the Commutative Property of Multiplication.



#### Support

Provide targeted intervention for students by using these resources.

If student response identifies: any choices other than A and D

#### Respond:

• Mini-Lesson | • 15 min Writing Two Expressions to Represent an Array



#### Strengthen

Reinforce students' understanding of the concepts assessed by using these resources.

If student response identifies: answers A and D with an explanation that the factors are the same

#### Respond:

• **Centers** | **4** 15 min Capture Squares, (Stage 5) Cover Up, (Stages 10 and 11) Match It, (Stage 1)



#### Stretch

Challenge students and extend their learning with these resources.

#### If student response identifies:

answers A and D with an explanation that the order of the factors does not affect the product

#### Respond:

• Sub-Unit 2 Extension Activities | 4 15 min





Support, Strengthen, and Stretch learning by assigning these digital resources that adjust to each student's current level of skill and understanding.

• Boost Personalized Learning • Fluency Practice • Math Adventures

#### **Math Language Development**

- EL Use the Math Language Development Resources for further language support with all your students, including those building English proficiency.
  - English/Spanish cognates e.g., factor/factor
  - English/Spanish Glossary e.g., product/producto
  - Frayer Model templates
  - Math Language Routine display structures, e.g., MLR8: Discussion Supports - Make a Conjecture
  - Vocabulary routines





#### **Professional Learning**

What part of the lesson went well today in terms of students' learning? What did you do that made that part go well?

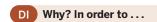
# Organizing Art Supplies

### Solving Problems With Arrays

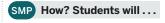
Let's analyze situations that involve arrays.

#### Focus on the Big Ideas

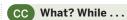
- - **1. Goal:** Write equations with a symbol for the unknown number to represent array story problems with unknown factors.
  - **2.** Language Goal: Solve story problems involving multiplication and explain strategies used. (Speaking and Listening)



Understand and explain arrays within contextual problems (DI1)



Use drawings of arrays to visualize the situation (SMP.1)



Writing an equation using a symbol for an unknown value. (CC2)

#### **Connections and Coherence**

Students solve contextual problems involving arrays and write multiplication equations to represent them. They consider which number represents the unknown value and then write equations using a symbol for the unknown. Students solve for the unknown using any strategy. (SMP.1, SMP.2)

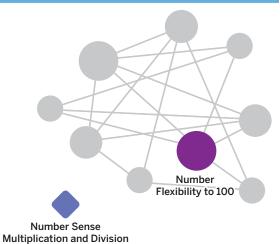
- Prior Learning CC2 Number Flexibility to 100 NS Multiplication and Division
  In Lesson 9, students represented multiplication situations with arrays and expressions.
- > Future Learning CC2 Number Flexibility to 100

In Lesson 11, students will use their understanding of arrays to plan different seating arrangements for a library reading event.

#### **Integrating Rigor in Student Thinking**

Students deepen their **conceptual understanding** of multiplication by representing array story problems with equations involving unknown values and **apply** multiplication to solve problems with unknown factors and products.

### **Today's Big Ideas**



#### Vocabulary

#### **Review Vocabulary**

array

### **S** CA CCSSM

#### Addressing

#### 3.OA.3

Use multiplication and division within 100 to solve word problems in situations involving equal groups, arrays, and measurement quantities.

Also Addressing: 3.OA.1, 3.OA.7

Mathematical Practices:~SMP.1,~SMP.2,~SMP.7,

SMP.8

CA ELD Standards: ELD.PI.3.1, ELD.PI.3.3,

ELD.PI.3.6, ELD.PI.3.12

### **Building Math Identity**

O I can be all of me in math class.

How are you like Harper in math class? How are you different?

Invite students to reflect on this question as they complete this lesson.

## Lesson at a Glance • 60 min

**S** CA CCSSM: 3.OA.1, 3.OA.3, 3.OA.7, SMP.1, SMP.2, SMP.7, SMP.8

#### Warm-Up Fluency

Whole Class | • 10 min

Students use the **Number Talk** routine, in which they look for structure and use repeated reasoning based on their own previous strategies or the strategies of others as they study a sequence of multiplication expressions with a factor of 2 and a factor that decreases by 1. (SMP.7, SMP.8)





#### **Activity 1**

(SMP.1, SMP.2)

1 Independent | 15 min

Students solve problems involving arrays that have an unknown amount of rows or an unknown amount in each row. Then they write multiplication equations to represent the problem and identify how each part of the equation represents it.

Manipulative Kit: connecting cubes or counters (as needed)







#### **Activity 2**

Pairs | 20 min

Students represent array problems by writing equations with symbols for unknown values. They then solve for the unknown value using any strategy. (SMP.2)

**Manipulative Kit:** connecting cubes or counters (optional)

**Materials:** Ways to Represent Multiplication Situations chart (from prior lesson)







### **Synthesis**

Whole Class | • 10 min

Students review and reflect on situations that could represent an array and strategies to solve for the unknown.

#### **Show What You Know**

♣ Independent | ● 5 min

Students demonstrate their understanding of the connections between arrays and multiplication equations by writing an equation with a symbol for the unknown value to solve a given problem.

Materials: Show What You Know PDF









#### **Math Language Development**

Multilingual/English Learners

Consider using the scaffolds from the Math Language Development Resources with Activity 1 to support math language acquisition for your students.

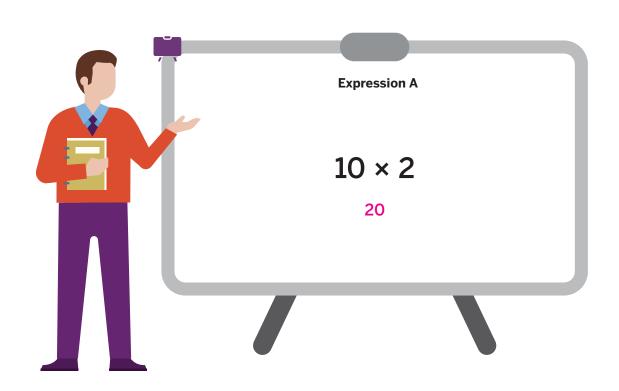


Emerging	Expanding	Bridging
Emerging text goes here.	Expanding text goes here.	Bridging text goes here.

### Warm-Up Number Talk

Lesson 10 Warm-Up

**Purpose:** Students evaluate multiplication expressions to look for patterns and begin to work toward fluency with multiplication facts in which 2 is a factor.



Expression B

 $9 \times 2$ 

18

**Expression C** 

 $8 \times 2$ 

16

**Expression D** 

 $7 \times 2$ 

14

**Why these problems?** These expressions provide an opportunity for students to recognize that as the first factor decreases by 1, the product decreases by 2.

### 1 Launch

Use the Number Talk routine.

**Display** 1 expression at a time.

**Say**, "Take your time to find the value mentally. Give me a signal when you have an answer and can explain how you determined it."



### 2 Connect

**Record** products and 2 or 3 strategies as students share, honoring all strategies and keeping expressions and work displayed.

**Repeat** with each expression, spending the most time discussing Expressions C and D.

Ask (if not yet mentioned during discussion), "What pattern can you determine as you look at all of the expressions and products? How can you explain why that is happening?"

### Students might say . . . § ELD.PI.3.1.Em, Ex, Br

A: I know 10 groups of 2 is 20.

**B:** 9 × 2 means 9 groups of 2, so I skip counted by 2 nine times and ended at 18.

C:  $9 \times 2$  is 18, so  $8 \times 2$  has to be 1 less group of 2. So,  $8 \times 2 = 16$ .

D: I notice that there is 1 less group of 2 each time, and the product goes down by 2 each time. So, 7 × 2 must be 14.

### **Activity 1** Array of Colors

**Purpose:** Students write a multiplication equation to represent problems involving arrays to identify what is unknown.

### Presentation Screens



#### **Materials**

#### Manipulative Kit:

 Provide students with access to connecting cubes or counters (as needed).

Short on time? Consider solving Problems 1 and 2 as a class.

### 1 Launch



**Read aloud** the introduction and Problems 1 and 2.

Say, "Complete Problems 1 and 2 independently and then discuss Problem 3 with a partner." (S ELD.PI.3.1.Em, Ex, Br

- Multilingual/English Learners Display a list of the words about the context that students might not know, such as *palette*. Include visuals or translations of each word in languages used by your students. (Reading and Listening)
- A **Accessibility: Visual-spatial processing** Provide connecting cubes or counters students can choose to use while solving the problem.

### 2 Monitor

After students have completed **Problem 3**, refer to the **Differentiation | Teacher Moves** table on the following page.



- Ask, "What are the numbers in this problem? What do each of the numbers represent?"
- Ask, "What information are you missing? How can you determine that missing information?"
- Multilingual/English Learners Emerging, Expanding, and Bridging scaffolds and supports are available in the *Math Language Development Resources*.

### 3 Connect



This Connect is structured using the MLR7: Compare and Connect routine.

Invite students to share their responses for Problem 3. ( ELD.PI.3.3.Em, Ex, Br

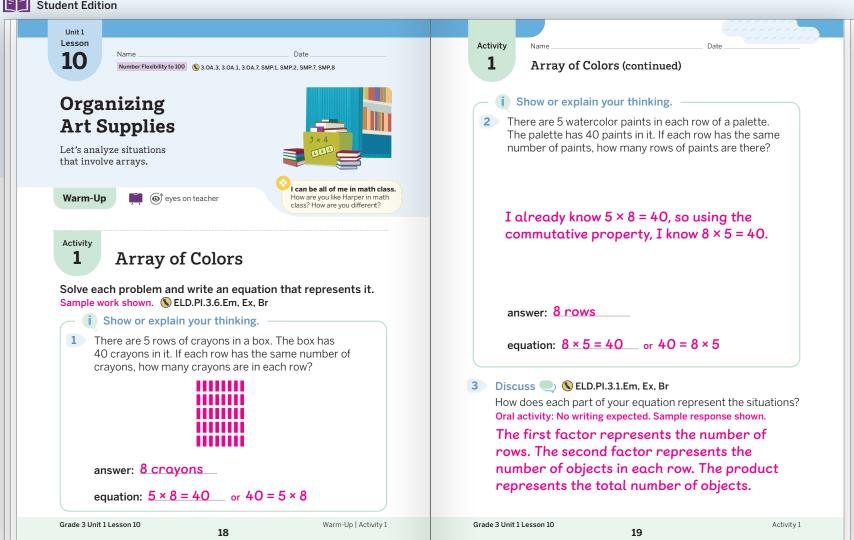
Use the Think-Pair-Share routine. Ask: (S) ELD.Pl.3.1.Em, Ex, Br

- "What is similar about these equations? What is different about these equations?"
- "What is the unknown value in the first equation? Second equation?" Consider circling the unknown value in each equation as students share.
- "How did you identify the unknown value in the situation?"



**Key Takeaway:** Say, "When given a multiplication situation involving arrays, sometimes you will determine an unknown number of rows or an unknown number of objects in each row."









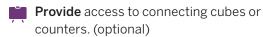
Look for students who	For example	Provide support
Almost there  Describe the numbers in general terms in their work.	5 is along the side, 8 is on the top, and 40 is all over.	Support Ask, "What does 5 represent? What does 8 represent? What does 40 represent?"
Relate each part of the equation as representing a different part of the multiplication situation.	5 represents the number of rows. 8 represents the number in each row. 40 represents the total.	Strengthen Ask, "What other multiplication equation could you write to match this situation?"
Relate each part of the equation as representing a different part of the multiplication situation and use the commutative property to relate the equation to another equation.	I can write 5 × 8 = 40 because there are 5 rows with 8 in each row. I can also write 8 × 5 = 40 because of the commutative property. I know that there are still 8 markers in 5 rows.	Strengthen Ask, "How does the equation you write to match the situation affect how you could solve for the unknown value?"

### **Activity 2** Arrays of Art Supplies

**Purpose:** Students identify the unknown in an array situation to be able to use a symbol to represent the unknown in an equation and then solve using any strategy.

### 1 Launch





**Read aloud** the directions and Problems 4 and 5.

Accessibility: Memory and attention Activate prior knowledge by having students refer back to previous activities in their Student Editions for strategies to solve similar problems.

Multilingual/English Learners Monitor and clarify any questions about the context. As students look over the problems, ask, "Are there any words or phrases that are unfamiliar? What questions do you have about any of the words or phrases?" SELD.PI.3.12.Em, Ex, Br

### 2 Monitor



After students have completed **Problem 5**, refer to the **O Differentiation | Teacher Moves** table on the following page.

### If students need help getting started . . .

- Suggest that students visualize the situation. Ask, "What representation does this problem make you think of?"
- Ask, "Tell me about the equation you wrote. How could you represent this equation with a drawing or an array?" Refer students to the *Ways to Represent Multiplication Situations* chart.

### 3 Connect



Invite students to share the equations they wrote and their solution strategies for Problem 5. Select and sequence their responses in the order shown in the Differentiation table.

Ask, "How did you decide what strategy to use to solve for the unknown?"

**Key Takeaway:** Say, "It can be helpful to think about a situation using an equation to represent what is known, what is unknown, and how those things are related. When you write an equation that represents what is known and unknown, you can use any strategy to solve for the unknown."



### **Materials**

#### Manipulative Kit:

Provide students with access to connecting cubes or counters (optional).

#### Classroom materials:

 Display the Ways to Represent Multiplication Situations chart (from prior lessons) throughout the activity.



Activity 2

Grade 3 Unit 1 Lesson 10

Almost there

known values.

20

They both have situations where a factor is unknown. However, in Problem 4, the second factor is unknown, which represents the number in each row. In Problem 5, the first factor is unknown, which represents the

Grade 3 Unit 1 Lesson 10

number of rows.

21

Activity 2

### D Differentiation | Teacher Moves



### Look for students who . . . For example . . .

<u>Support</u> Ask, "What does the unknown amount in the equation represent?"

Provide support . . .

Create an array or equal groups to determine the unknown value.

Determine the product of the

•••••

There are 2 rows of colors.

Strengthen Ask, "How did you know this strategy would work? How would your strategy change if you knew the number of rows but did not know the number of colors in each row?"

Use the structure of their equation to reason about and calculate the unknown value.

The unknown value is the number of groups. So I thought about how many groups of 7 are in 14. There are 2 groups of 7 in 14, so there are 2 rows of colors.

Stretch Say, "You said there are 2 groups of 7 in 14. You could represent that as 7 + 7 = 14 or as  $2 \times 7 = 14$ . Compare these equations and talk about how they relate to each other."

Presentation Screen



### **Synthesis**

Lesson Takeaway: Problems involving rows or columns can be represented with multiplication equations, using a symbol for the unknown value. Different strategies can be used to determine the missing value.



### Ask:

- "What situation could this image be about?"
- "How could you represent that situation with an equation to represent the unknown?"
- "How would you solve for the unknown value?"

Say, "You will continue thinking about how the structure of arrays relates to factors, products, and equations in the next lesson."

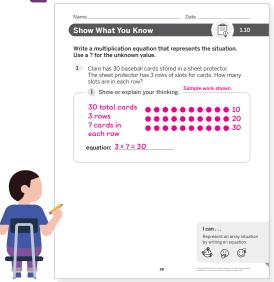
Invite students to refer to the Summary during Practice or anytime during the year.

### Show What You Know Independent | 4 5 min

Students using digital

Lesson 10 Show What You Know





### Today's Goals

- 1. Goal: Write equations with a symbol for the unknown number to represent array story problems with unknown factors.
  - In the Show What You Know, students write an equation to represent an array story problem using a symbol to represent an unknown
- 2. Language Goal: Solve story problems involving multiplication and explain strategies used. (Speaking and Listening)

Differentiation

See the last page of the lesson for differentiation and Math Language Development support.

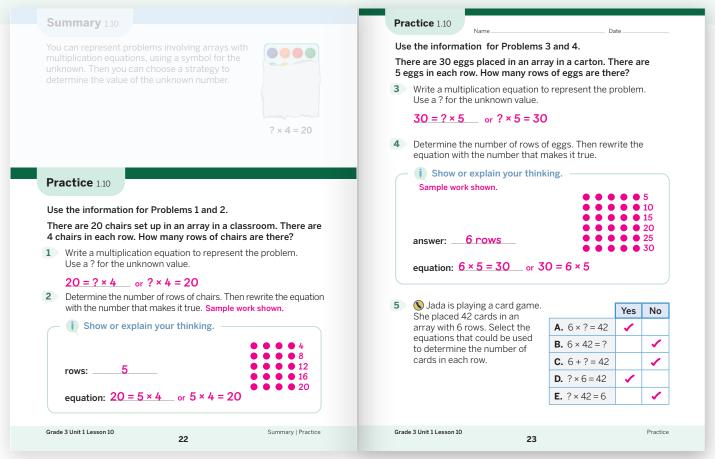
#### **Practice** Independent

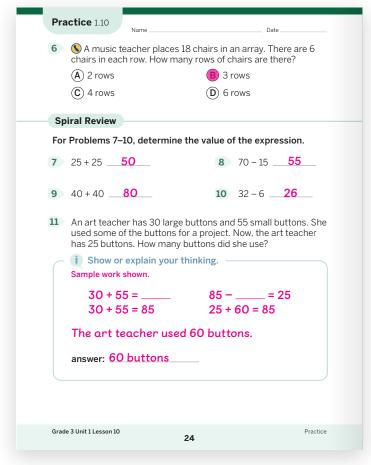
Provide students with sufficient practice to build and reinforce their conceptual understanding, fluency, and application of mathematical topics, assessment practice, and ongoing spiral review.

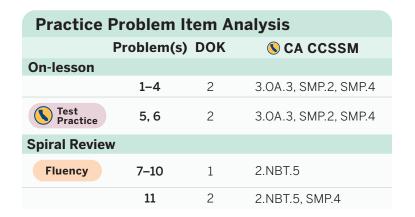


Students using digital











Additional practice can be found in the Practice Resources. Intervention, Extension, and Investigation Resources, and online resources (item banks, Boost Personalized Learning, and Fluency Practice).

Lesson Goal: Write equations with a symbol for the unknown number to represent array story problems with unknown factors.



### **Support**

Provide targeted intervention for students by using these resources.

If student response identifies: an equation other than  $3 \times ? = 30$  or  $3 \times 10 = 30$ 

#### Respond:

• Mini-Lesson | • 15 min Relating Array Situations to Equations



### Strengthen

Reinforce students' understanding of the concepts assessed by using these resources.

If student response identifies:  $3 \times 10$  $= 30 \text{ or } 30 = 3 \times 10$ 

#### Respond:

• Center | **4** 15 min Capture Squares, Stage 5 Cover Up, Stage 11 Match It, Stage 1





### **Stretch**

Challenge students and extend their learning with these resources.

If student response identifies:  $3 \times ? =$ 30 or 30 = 3 x?

#### Respond:

• Sub-Unit 2 Extension Activities | 4 15 min





Support, Strengthen, and Stretch learning by assigning these digital resources that adjust to each student's current level of skill and understanding.

• Boost Personalized Learning • Fluency Practice • Math Adventures

### **Math Language Development**



L Use the **Math Language Development Resources** for further language support with all your students, including those building English proficiency.

- English/Spanish cognates
- English/Spanish Glossary e.g., array/formación
- Frayer Model templates
- Math Language Routine display structures, e.g., MLR7: Compare and Connect
- Vocabulary routines





### **Professional Learning**

Who has been sharing their ideas in class lately? Make a note of students whose ideas have not been shared and look for an opportunity for them to share their thinking in the next lesson.

# A Community Reading Event

# Different Representations of Multiplication

Let's see how Harper can use math in her reading community.

### Focus on the Big Ideas

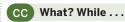
- - 1. Goal: Represent and solve real-world problems involving arrays.
  - **2.** Language Goal: Explain how arrays represent real-world multiplication situations. (Speaking and Listening)



Make sense of real-world problems involving multiplication (DI1)



Use mathematical modeling to represent seating arrangements (SMP.4)



Generating expressions and arrays. (CC2)

### **Connections and Coherence**

Students create arrays to represent real-world situations, applying what they know about the Commutative Property of Multiplication while reasoning through different configurations for real-world scenarios. They are introduced to a new stage of the Center *Cover Up*, in which they are given the opportunity to build fluency as they multiply with factors 1–5 and 10. (SMP.1, SMP.4, SMP.8)

Prior Learning CC2 Number Flexibility to 100 NS Multiplication and Division

In Lesson 10, students used equations and arrays to represent and solve problems using symbols for unknown values.

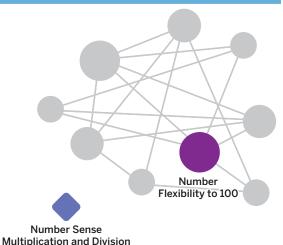
> Future Learning CC1 Represent Multivariate Data

In Unit 2, students will continue to explore the concept of multiplication as it relates to another new concept — the area of two-dimensional shapes.

### Integrating Rigor in Student Thinking

Students **apply** their understanding of representing multiplication in real-world scenarios, building **strategies for computation** with multiplication involving factors of 1–5 and 10, reducing reliance on models to determine products.

### **Today's Big Ideas**



### Vocabulary

#### **Review Vocabulary**

arra

Commutative Property of Multiplication

### **S** CA CCSSM

#### Addressing

#### 3.OA.3

Use multiplication and division within 100 to solve word problems in situations involving equal groups, arrays, and measurement quantities.

Also Addressing: 3.0A.7

Mathematical Practices: SMP.1, SMP.4, SMP.7, SMP.8

Building On Building Toward
2.NBT.5 3.NBT.2

CA ELD Standards: ELD.PI.3.1, ELD.PI.3.3, ELD. PI.3.6, ELD.PI.3.9

### **Building Math Identity**



What makes your math class a community? How are you a part of that community?

Invite students to reflect on this question as they complete this lesson.

### Lesson at a Glance • 60 min

**S** CA CCSSM: 3.OA.3, 3.OA.7, SMP.1, SMP.4, SMP.7, SMP.8

### Warm-Up Fluency

Whole Class | • 10 min

Students use the **Number Talk** routine, in which they look for structure and use repeated reasoning based on their own previous strategies or the strategies of others as they study a sequence of related subtraction expressions. **(SMP.7, SMP.8)** 





### **Activity 1**

Small Groups | 4 20 min

Students explore a real-world application of arrays as they design seating arrangements for a changing number of attendees at a reading event using arrays. They examine the work of others by participating in a **Gallery Tour. (SMP.1, SMP.4)** 

Manipulative Kit: inch tiles (as needed)

Materials: tools to create a visual display







### **Activity 2**

Pairs | • 15 min

Students are introduced to the Center *Cover Up, Stage 12*, in which they determine the product of 2 numbers. Students use repeated reasoning to build fluency by writing and evaluating expressions involving factors of 1–5 and 10. **(SMP.8)** 

**Manipulative Kit:** base-ten units, counters, inch tiles (as needed)

Centers Resources: Gameboards A and B











### **Synthesis**

Whole Class | • 10 min

Students review and reflect on the work of the lesson and the sub-unit, including how equal groups, arrays, expressions, and equations represent multiplication.





### **Show What You Know**

å Independent | ● 5 min

Students demonstrate their understanding by representing a real-world situation with an array and a multiplication equation.

Materials: Show What You Know PDF







#### **Math Language Development**



Consider using the scaffolds from the Math Language Development Resources with Activity 1 to support math language acquisition for your students.



### Emerging

Students make sense of real-world problems using a graphic organizer and sentence frames.

Guided questions are provided for you to ask for students to share one-word responses.

### Expanding

Students make sense of real-world problems using a graphic organizer and sentence frames.

Guided questions are provided for you to ask for students to share simple phrases.

#### Bridging

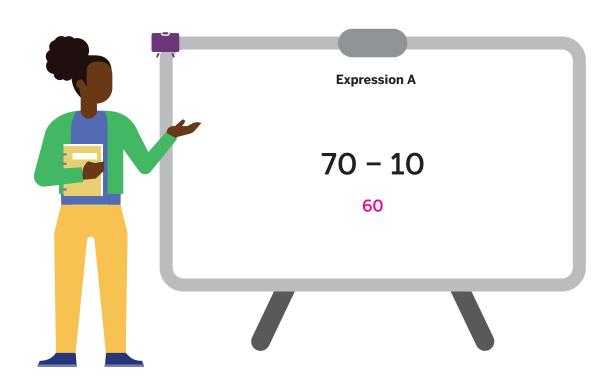
Students make sense of real-world problems using a graphic organizer and sentence frames.

Guided questions are provided for you to ask for students to share responses using longer phrases or complete sentences.

### Lesson 11 Warm-Up

### Warm-Up Number Talk Fluency

**Purpose:** Students subtract related pairs of numbers to practice and develop fluency with subtraction within 100.



**Expression B** 

68 - 10

58

**Expression C** 

70 - 12

58

**Expression D** 

68 - 12

56

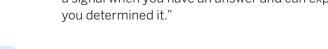
Why these problems? These expressions lend themselves to using subtraction strategies based on place value.





**Display** 1 expression at a time.

**Say**, "Take your time to find the value mentally. Give me a signal when you have an answer and can explain how you determined it."

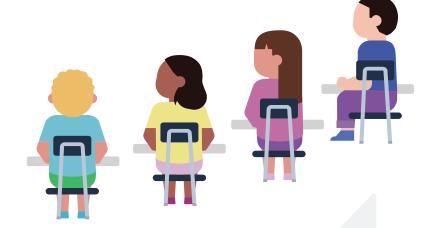


### 2 Connect

**Record** differences and 2 or 3 strategies as students share, honoring all strategies and keeping expressions and work displayed.

**Repeat** with each expression, spending the most time discussing Expression D.

**Ask**, "How can you use Expressions B or C to help you find the value of Expression D?"



### Students might say . . . . S ELD.PI.3.1.Em, Ex, Br

- A: I know 7 tens minus 1 ten is 6 tens.
- B: It's just like the first one, but the number you are subtracting from is 2 less. So, the difference would be 2 less, which is 58.
- C: This is like the first problem, but you are subtracting 2 more from 70. So, instead of 60, it is 58.
- D: 68 is 2 less than 70, so the answer is 2 less than 70 minus 12, which is 56.

### **Activity 1** Seating Situations

**Purpose:** Students create arrays that represent seating arrangements. They examine classmates' arrays to consider others' reasoning for creating different configurations that represent a real-world situation.

### Launch



**Ask**, "Think of an event you attended where chairs were set up for people to sit. What do you remember about how the chairs were arranged?"

**Read aloud** the introduction and Problem 1.

Have students complete Problem 1 and then pause for a class discussion.

Invite 2-3 students to share their arrays. Ask, "What equation could represent how you arranged the chairs?"

MLR6: Three Reads Read the story problem aloud 3 times.

Read 1: Say, "Tell your partner what the situation is about without using any numbers."

Presentation Screens

**Materials** 

Manipulative Kit:

(as needed). Classroom materials:

· Provide students with access to

inch tiles during the Monitor

Distribute tools for students to

create a visual display.

Lesson 11 **Activity 1** 

- Read 2: Ask, "What values are known and what values are unknown?"
- Read 3: Ask, "How could you use the relationship between these values to solve the problem? \(\subseteq\) ELD.PI.3.6.Em, Ex, Br

Read aloud Problems 2 and 3.

### **Monitor**



After students have completed **Problem 2**, refer to the D Differentiation | Teacher Moves table on the following page.

#### If students need help getting started . . .

- Ask, "Tell me about the number 36. How can 36 be shown with equal groups?"
- For Problem 2, ask, "What do you know now about the number of people coming? What problem does Harper have?"
- **Accessibility:** Visual-spatial processing Provide access to inch tiles to model the seating arrangements in the student-facing task statement. Students can move the tiles to reflect the changes happening from Problem 1 to Problem 2.
- Multilingual/English Learners Emerging, Expanding, and Bridging scaffolds and supports are available in the *Math Language Development Resources*.

### Connect



- Use the Gallery Tour routine. Say, "We will do a Gallery Tour. You will take a tour around our classroom to look at your classmates' work and have a discussion with your group. As you look at the representations, think about what is similar and what is different."
- Invite students to share their reasoning behind their arrays and why they organized the chairs the way they did given the context.

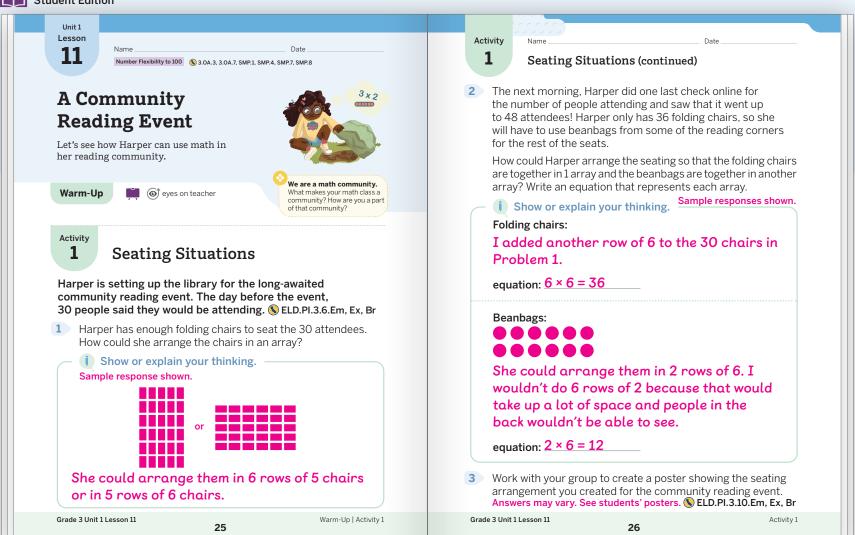
S ELD.PI.3.9.Em, Ex, Br

Ask, "Why do you think arrays are often used in these kinds of situations, like arranging chairs or other objects?



**Key Takeaway:** Say, "You can make arrays for different totals using the same number of rows or the same number of columns — both of which makes them helpful to organize or arrange things in real-world situations. Depending on the context, it may make more sense to have 1 array arrangement than another."









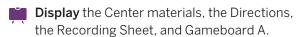
Look for students who	For example	Provide support
Use trial and error strategies to build the arrays.	I tried rows of 5 first, but I had 1 left over. Then I tried rows of 6, and it worked with 6 rows.	Strengthen Say, "Describe the array and how you determined the equal rows and equal columns."
Represent the 36 folding chairs and 12 beanbags, reasoning about the 2 seating arrangements independently of each other.	I arranged the inch tiles in 3 rows of 12. I arranged the counters in 2 groups of 6.	Strengthen Ask, "What is another way that the seating could be arranged?"
Think about how the context of the situation affects their arrangements.	I could do 6 rows of 2 for the beanbags, but people toward the back might not be able to see the reader. I think 2 rows of 6 would be better so everyone is close to the reader.	Strengthen Ask, "Why is it important to think about the situation while you think about the math?"

### **Activity 2** Introducing the Center Cover Up, Stage 12

Purpose: Students play a game to practice multiplying with factors of 1–5 and 10.

### Launch





Demonstrate how to play Cover Up, Stage 12 by inviting a student to act as a partner. While demonstrating:

- Say, "You are going to play Cover Up."
- Say, "First, I need to place each cube on a number in the gray row.'
- Use the Think-Pair-Share routine. Ask, "2 and 4 are the factors. What multiplication expression can I write using these numbers? How could I determine the product of this expression?" Record 1 or both possible expressions and the product on the Recording Sheet. ( ELD.PI.3.1.Em, Ex, Br
- Say, "Next, I cover the product with a counter."
- Say, "Now, my partner will move one of the cubes, multiply the 2 numbers, and cover the product, if it is not already covered. Then my partner will record the expression and product on the Recording Sheet. Take turns playing the game. The first player to cover 5 squares in a row wins."



**Accessibility:** Visual-spatial processing Provide inch tiles or other objects students can choose to use while playing the game.

### **Monitor**



If students need help getting started . . .



Ask, "When multiplying 2 numbers, what does the first factor represent? What does the second factor represent?"

### Connect



Invite students to share strategies they used to determine the value of expressions in the order shown in the Differentiation table.

- "Did you use this strategy every time?"
- "Which strategy do you prefer? Why?"



Key Takeaway: Say, "You can calculate the product of 2 numbers using strategies, such as representing the equal groups and counting all, skip counting, repeated addition, or using other known products."

#### Presentation Screens



### **Materials**

#### Manipulative Kit:

· Distribute two base-ten units, inch tiles (as needed), and 25 two-color counters to each pair.

#### Centers Resources:

Distribute Gameboards A and B to each pair.



Short on time? Consider reducing the amount of time students play the game. number. Multiply the numbers.

 Place each cube on a number in the gray row. Each cube can be on a different number, or both cubes can be on the same

Cover the product of the two numbers with a counter.Record the multiplication expression and product.

If the product is not already covered with a counter, cover it.
Record the multiplication expression and product.

(6) **How to Win** The first player to cover 5 squares in a row wins.

27

Take turns moving one cube at a time. Record each multiplication expression and product, even if you were unable to cover the

• Move one of the cubes. Multiply the numbers.

How to Play
Player A:

Grade 3 Unit 1 Lesson 11

CENTER Recording Sheet

ame \_\_\_\_\_

Cover	Up	(continued)

Multiplication expression	Product

28

## D Differentiation | Teacher Moves



Activity 2

Create an equal-groups drawing or

Look for students who . . .

array to represent 5 groups of 4 objects and then count by 1 to determine the product.

For example . . .  $(5 \times 4)$ 

Grade 3 Unit 1 Lesson 11

Activity 2

1, 2, 3, 4, 5, 6,..., 20

Provide support . . .

in each [group, row, or column]? If you know there are 4 dots in each group, how could you determine the total without counting each dot one by one?"

Determine the product using skip counting or repeated addition.

• • • • • 10 • • • • • 15 • • • • • 20

5 + 5 + 5 + 5 = 20

strengthen Ask, "What other products do you know with 4 or 5 as a factor? How could you use those known products to help you determine the value of this expression?"

Use an expression or product from a previous turn to calculate the product.

I found  $4 \times 4 = 16$  for another turn.  $5 \times 4$  means I can add another 4 to 16 to get 20. So,  $5 \times 4 = 20$ .

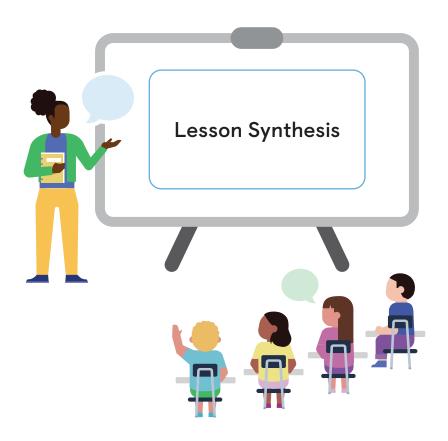
Stretch Ask, "How could you determine the product of 6 × 4? How could you determine the product of 8 × 4?"

Presentation Screen



### **Synthesis**

Lesson Takeaway: Arrays can show different ways objects can be arranged in equal groups, making real-world situations visually clear. Many strategies can be used to determine the product of 2 numbers.



Say, "You saw many strategies you can use when multiplying."

Ask, "Where do you see each strategy represented in this array?"

Say, "In this sub unit, you worked with arrays to represent multiplication. Throughout the year, you will continue to build on your understanding of multiplication."

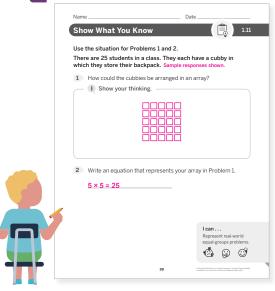
Invite students to refer to the Summary during Practice or anytime during the year.

### Show What You Know Independent | 4 5 min

Students using digital

Lesson 11 Show What You Know





### ■ Today's Goals

- 1. Goal: Represent and solve real-world problems involving
  - In the Show What You Know, students solve a real-world problem involving multiplication using an array.
- 2. Language Goal: Explain how arrays represent real-world multiplication situations. (Speaking and Listening)

See the last page of the lesson for differentiation  $and\ Math\ Language\ Development\ support.$ 

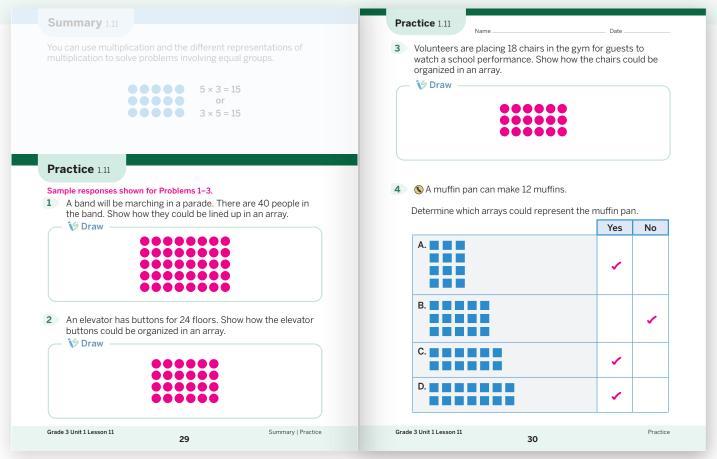
### Practice Independent

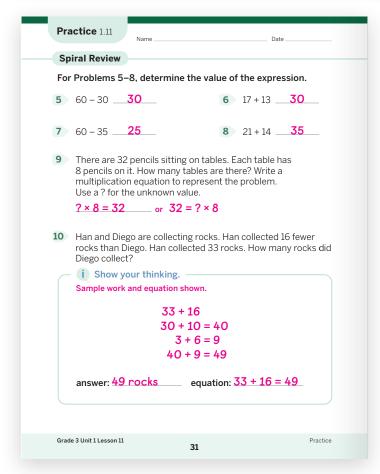
Provide students with sufficient practice to build and reinforce their conceptual understanding, fluency, and application of mathematical topics, assessment practice, and ongoing spiral review.

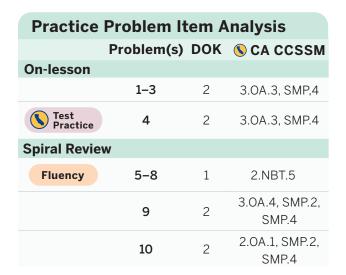


Students using digital

#### Students using print









Additional practice can be found in the **Practice Resources**, **Intervention, Extension, and Investigation Resources**, and online resources (item banks, Boost Personalized Learning, and Fluency Practice).

**Lesson Goal:** Represent and solve real-world problems involving arrays.



#### **Support**

Provide targeted intervention for students by using these resources.

**If student work shows:** more or less than 20, or unequal groups

#### Respond:

• Mini-Lesson | • 15 min Solving Multiplication Problems Using Arrays

### Strengthen

Reinforce students' understanding of the concepts assessed by using these resources.

**If student work shows:** 20 arranged into an array

#### Respond:

Centers | 15 min
 Capture Squares, Stage 5
 Cover Up, Stage 11
 Match It, Stage 1

### S

### Stretch

Challenge students and extend their learning with these resources.

**If student work shows:** any of the following equations:  $4 \times 5 = 20$ ,  $5 \times 4 = 20$ ,  $2 \times 10 = 20$ ,  $10 \times 2 = 20$ 

### Respond:

• Sub-Unit 2 Extension Activities | 4 15 min







### **Math Language Development**



- English/Spanish cognates
- English/Spanish Glossary e.g., array/formación
- Frayer Model templates
- Math Language Routine display structures e.g., MLR6: Three Reads
- Vocabulary routines



#### **Professional Learning**

How did creating the visual display for the Gallery Tour support collaboration between students?

# Sub-Unit Summary

### Sub-Unit 2 | Summary



Sub-Unit Summaries and other helpful resources can be accessed on the Caregiver Hub at amplify.com/caregiver-hub.

#### In this sub-unit . . .

 We discovered that arrays are related to equal groups and to multiplication. We represented arrays with expressions and equations.

### **Equal groups**









### Expression

3 × 5

**Equation** 

 $3 \times 5 = 15$ 

- Math tip: The rows and columns of arrays show equal groups. When representing arrays with expressions, you can think about the factors as the number of rows (or columns) and the number of objects in each row (or column).
- Using our understanding of arrays, we saw that we can multiply numbers in any order and still get the same product. This is called the <u>Commutative Property of</u> <u>Multiplication</u>.

$$3 \times 5 = 15$$

$$5 \times 3 = 15$$

$$3 \times 5 = 5 \times 3$$

Grade 3 Unit 1

Sub-Unit 2 | Summary

Notes:

Notes	

Notes			

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### Amplify.